

### Lecture-7

#### Application of Heisenberg's Uncertainty Principle:

##### **i. The non-existence of free electron in the nucleus.**

The diameter of nucleus of any atom is of the order of  $10^{-14}$  m. If any electron is confined within the nucleus then the uncertainty in its position ( $\Delta x$ ) must not be greater than  $10^{-14}$  m.

According to Heisenberg's uncertainty principle,

$$\Delta x \Delta p \geq h / 2\pi$$

The uncertainty in momentum is

$$\Delta p \geq h / 2\pi \Delta x, \text{ where } \Delta x = 10^{-14} \text{ m}$$

$$\Delta p \geq (6.63 \times 10^{-34}) / (2 \times 3.14 \times 10^{-14})$$

$$\text{i.e. } \Delta p \geq 1.055 \times 10^{-20} \text{ kg-m / s}$$

This is the uncertainty in the momentum of electron and then the momentum of the electron must be in the same order of magnitude.

##### **ii. Width of spectral lines (Natural Broadening)**

Whenever a photon interacts with matter the atoms get excited and the excited atom gives up its excess energy by emitting a photon of certain frequency which leads to the spectrum. The broadening in the spectral lines is observed due to the indeterminateness in the atomic energies. According to Heisenberg's uncertainty relation

$$\Delta E = \frac{h}{2\pi \Delta t}$$

where  $\Delta E$  is the uncertainty in the measurement of energies and  $\Delta t$  is the mean life time of the level is finite ( $10^{-8}$  secs). Therefore  $\Delta E$  must have a finite energy spread that means the energy levels are not sharp and hence the broadening of the spectral lines.